

# The Quantum Key Distribution, Attenuation and Propagation over Ocean Surface for Various Naval Applications

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**Abstract**—The quantum encryption is a method of key transfer in cryptography by using quantum entanglement of photons. The real power of quantum entanglement is instantaneous communication that is non-interceptable. The advantage of quantum encryption method is, it can be incorporated with conventional encryption methods safely. The quantum cryptography can replace conventional key exchange mechanism with the polarized photons using channels like optic fiber cables. Quantum cryptographic can also provide far and secure data communication. The present day experiments clearly proved that the quantum cryptography can be implemented through medium like optic fiber cable or air. But the distance of transmission through the air is limited by rule of line of sight propagation. The quantum key distribution will have uses in different types of communication between distant parts of earth. So this paper discussing how the visual horizon affect the quantum key distribution in naval applications

**Keywords:** Quantum cryptography, Communication network, Free-space optical communication

## I. INTRODUCTION

The research on quantum cryptography is critical for future fully secured communication needs. The quantum encryption can create codes that are unbreakable with non-interceptable Quantum key distribution schemes. Because of this feature quantum encryption systems is considered as more secure and safer. The computing power of quantum computers increasing as compared with conventional computing systems and so can be used for breaking currently existing key distribution scenarios [1]. The different malicious activities and crimes are increasing over the communication networks. The attacks over the critical computer networks causes huge losses and it also challenging the security of nations. The implementation of quantum key encryption can significantly improve the security of communication networks. So this work can help to improve the security in communication systems. Since the quantum cryptography mainly relied on polarized photons the transmission is limited to the line of sight and hence here we discuss the various aspect of this propagation over the surface of earth. calculated horizon for Quantum cryptography link when using in various type of naval vessels. This paper successfully verified the theoretical formula of horizon calculation of Quantum Key Distribution devices for using

in various naval vessels by an experimental setup. However the theoretical equation for Power loss and Data rate have to be verified for Quantum cryptography link using polarized photons with suitable experimental setup in future work.

## II. QUANTUM CRYPTOGRAPHY AND THE EVOLUTION

In early 1980s, Bennet C, Benioff P, Feynman R proposed that a new powerful way of information processing was possible with quantum states. Richard Feynman was proposed this idea in 1981 that quantum systems could be performed powerful than classical computing [3], and thus the concept of quantum computing was originated. David Deutsch was further studied it and published a paper in 1985 [4]. However the origin of quantum cryptography was considering to be started since 1983 from the work of Weisner [5], when he proposed single quantum states had to be used for information transmission.

In 1989, Deutch published another paper "Quantum computational networks" [6] and proposed a new quantum idea that quantum gates can combine for quantum computation so that boolean gates could be achieved

computation and so similarly quantum circuits also. The major advancement in theoretical quantum cryptography was considered to be happened in 1991 when Ekert suggested that Einstein- Podolsky- Rosen[7], two - particle state of entanglement could be used to establish quantum cryptography state

### III. QUANTUM KEY DISTRIBUTION BASED COMMUNICATION LINK

The quantum key distribution based communication link(QKD Link) between the Alice and Bob can be represented as the figure 1 below. The quantum channel is used for establishing secure quantum cryptography based key transfer. The classical channel is used for the conventional data transfer between the devices by any medium like optic fiber cables or air.

The quantum channel is used for sending the key between source and destination[8] by using the polarization of photons and corresponding bit values zero or one as the figure 2 represents. The photons can be either Rectilinear or Diagonal polarization mode and hold the value of zero or one. Detector can retrieve this bit values by checking the polarization state of received photons

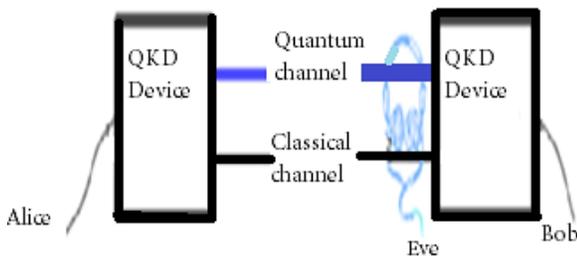


Figure1. Quantum key distribution based communication

#### A. Quantum key distribution based data transfer

Alice and Bob perform the quantum key distribution as per the below steps[8]

- (i) Alice communicates with Bob through the quantum channel by sending the polarized photons.
- (ii) Then both of them discuss results using a public channel
- (iii) Then after receiving encryption key Bob can encrypt the messages and communicate through any public channel. If any attempt at eavesdropping will not only be unsuccessful but also an incorrect reading would destroy information and also Bob and Alice no longer would have the same key because of

information already loss and eventually eavesdropper's presence could be known to both parties .

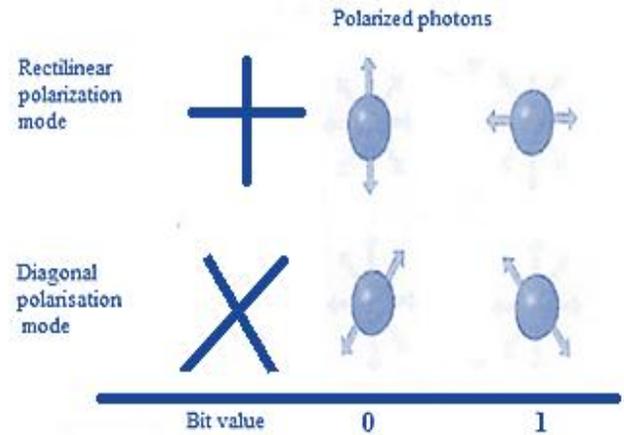


Figure 2. Polarized photons and corresponding bit values

### IV. Quantum cryptography possibilities of communication over the ocean surface

- (i)The QKD(Quantum Key Distribution) can be used for secure communication between ships to command center via satellite
- (ii) The QKD can be used for communication between the command center to the aircraft from a remote location
- (iii)The QKD between the ship to ship or aircraft is limited within the visible horizon due to QKD uses polarized photons for communication.

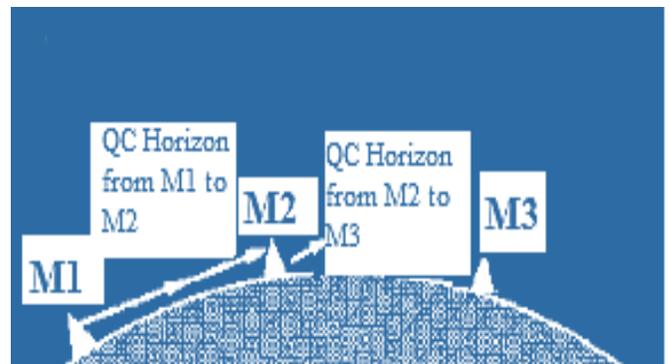


Figure-3. Quantum cryptography (QC) horizon from different points over earth surface M1 to M2 and M2 to M3

### V. THE QUANTUM CRYPTOGRAPHY LINK HORIZON CALCULATION

The horizon or skyline is the apparent line that separates earth from sky, the line that divides all visible directions

into two categories: those that intersect the earth's surface, and those that do not. At many locations, the true horizon is concealed by trees, tall buildings, mountains, etc. but it is clearly visible in ocean and the resulting intersection of earth and sky is termed as the visible horizon. Historically, the distance to the visible horizon has long been critical for the successful navigation at sea, because it determined an observer's maximum range of visibility[9] and similarly for Line of sight propagation of Quantum Key Distribution. This importance had been became less significant due to the development of the radio communication systems but today and future, the horizon calculation can become again significant due to Quantum Cryptography based communication.

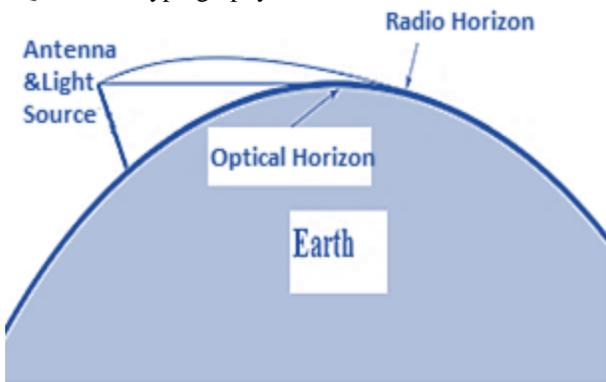


Figure 5. Optical and Radio Horizon

The radio horizon is the locus of points at which direct rays from an antenna are tangential to the surface of the Earth. If the Earth was a perfect sphere and there was no atmosphere, the radio horizon would be a circle. The radio horizon of the transmitting and receiving antennas can be added together to increase the effective communication range.

In astronomy the horizon is the horizontal plane of the observer. It is the fundamental plane of the horizontal coordinate system, the locus of points that have an altitude of zero degrees. While similar in ways to the geometrical horizon, in this context a horizon may be considered to be a plane in space. This importance of Light spectrum using for communication purpose was reduced due to the development of the radio communication systems, but now and future, the horizon calculation can become again significant due to Quantum Cryptography based communication system, which can provide high security in data transfer using polarized photons.

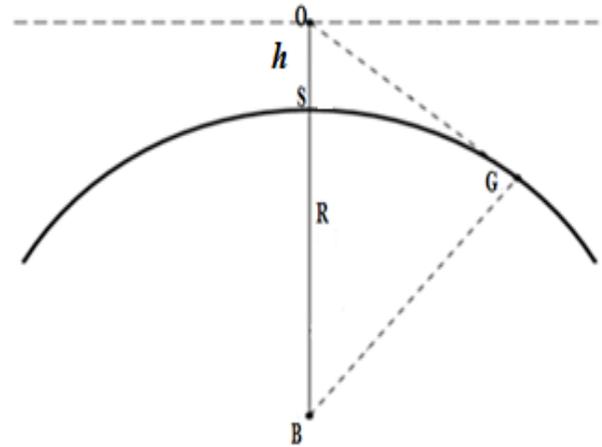


Figure-4 .Geometrical horizon calculation

The horizon for QKD transmission can be calculated at a point 'O' to the point G by the Pythagoras theorem[10]

$$(R + h)^2 = R^2 + BG^2, \text{ Where } BG = OG$$

$$\text{So } (R + h)^2 = R^2 + OG^2$$

$$\text{So } OG^2 = (R + h)^2 - R^2 \text{ expand term } (R + h)^2 \text{ we get } R^2 + 2 R h + h^2,$$

$$OG^2 = (R^2 + 2 R h + h^2) - R^2 \text{ so that}$$

$$OG^2 = 2 R h + h^2 \text{ and we get}$$

$$OG = \sqrt[3]{(2 R h + h^2)}$$

when calculating earth horizon  $h < R$ , so that can neglect the second term  $h^2$ .

So we get finally get the OG as  $OG = \sqrt[3]{2 R h}$ , using kilometers for d and R, and meters for h, and taking the radius of the Earth as 6371 km, the distance to the horizon is

$$\sqrt{(2 * 6371 * h)/1000} \text{ is approximately equal to}$$

$$3.570\sqrt{h} \text{ is the equation}$$

Examples, assuming no refraction:

- i. For an observer on the ground with his eye level at  $h = 1.70$  m, the horizon can be calculated by substituting in above equation and the answer is 4.655 km.
- ii. For any observer standing on a hill top or a tower of 50 m in height, the horizon would be at a distance of 25.24 km
- iii. For an observer standing over a mountain with 5000 m in height, the horizon will be at a distance of 252 km approximately.
- iii. For a pilot, who flying in a plane at 10000 m, the horizon will be at a distance of 357 km with neglecting the

effect of refraction of the light that passing through the air. Distance to horizon calculations gives an idea how far away an object that visible for the line of sight propagation. The refractive error on Earth's curved surface causes an error in geometric calculation. When any ground, water or surface is colder than the air above which cause a dense layer of air forms close to the surface and so light bends downward while traveling. The reverse phenomena happens when the ground is hotter than air above it, usually happening at desert environment.

**VI. APPROXIMATE COMPENSATION FOR REFRACTION IN QUATUM KEY DISTRIBUTION**

The atmosphere bends light while travelling through the atmosphere due to the refraction of light but the rate of bending is unpredictable and never be a constant value. This is because of the variation of temperature and pressure in the atmosphere. So when measuring longer distances over the horizon in an ocean surface, increase R by the 15-20% from the calculated horizon value and ensure line of sight is at least 5 feet from the surface, for reducing random errors created by refraction.

To compute the maximum distance at which an observer can see the top of an object floating in ocean surface ,then add this height h for the calculation as  $d = \sqrt{2Rh + h^2}$

Where R is the radius of the Earth, where R and h must be in the same units. Consider an example, when a satellite revolving presently at a height of 1500 km, then distance to the horizon will be at 4372 kilometers .So the r random errors created by refraction can be calculated by increasing R by 20% of the value as follows.

20% increase of 6371 km is 7645

$$\sqrt{(2 * 7645 * 1500) + 1500 * 1500}$$

$$= 5018.47\text{km}$$

**VII. QUANTUM CRYPTOGRAPHY LINK HORIZON CALCULATION FOR A SATELLITE BASED QUANTUM KEY DISTRIBUTION DEVICES**

The quantum cryptographic link between any naval vessels is limited by the line of sight propagation of photons.

However it can be resolve by using the satellite nod between communication entities, but possibility is that each node must have to completely process polarized photons and have to establish a fresh quantum key distribution link between each node to node as per the law of quantum mechanics that polarization state of particles can measure only once without changing its state.

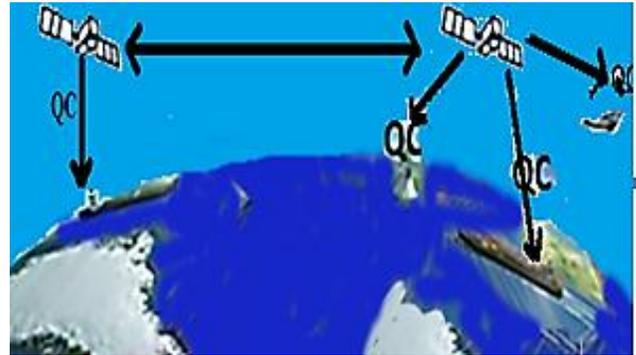


Figure-7. A method for beyond horizon Quantum key distribution, where QC is Quantum key distribution (QKD) links from satellite to ship, Satellite to aircraft, Command station to satellite. CC is commanding center

When height h is significant with respect to R for the case of most satellites, then the approximation of calculation for simplicity made previously will be no longer valid and so the exact formula is required, So that the Line of sight d can be calculated as  $d = \sqrt{2Rh + h^2}$

where R is the radius of the Earth ,where R and h must be in the same units. Consider an example, when a satellite revolving presently at a height of 1000 km, then distance to the horizon will be at 4372 kilometers.

So the r random errors created by refraction can be compensated by increasing 20% R of the value, So horizon can be calculated as follows.

20% increase (because of 'h' is large as 1500km) to the 6371 km is 7645km. So Horizon OG =

$$\sqrt{(2 * 7645 * 1000) + 1000 * 1000}$$

$$= 4188\text{km}$$

So 4188km is the horizon for a quantum key distribution link of a satellite revolving 1000km

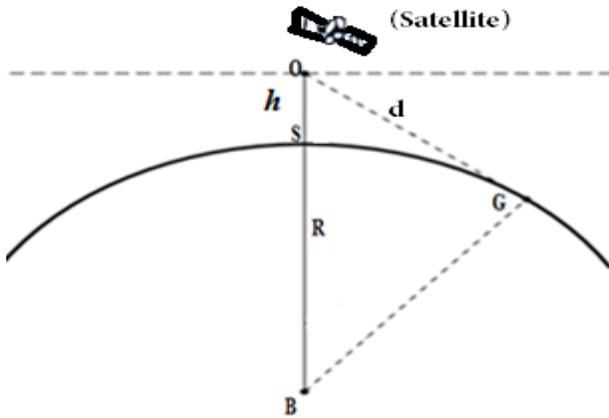


Figure-8. Quantum Key Distribution Horizon from a Satellite

**VII. THE QUANTUM CRYPTOGRAPHY (QC) LINK HORIZON CALCULATION FOR HAND HELD QUANTUM KEY DISTRIBUTION (QKD) DEVICES WHEN USING OVER NAVAL VESSELS**

The initial success of achievement of reducing the size of components as well as higher key generation rates could be achieved while making the pocket size Quantum key distribution . That module will be an attractive add-on to conventional wireless methods. Such an integrated photonics platforms could enable secure communication with handheld devices such as smartphones. The work of Gwenaelle Vest, Markus Rau, Lukas Fuchs[11] presented a new design for a system where Alice(One user) owns a mobile Quantum key distribution unit, which allows her to perform secure free-space communication with any type of Quantum key distribution receiver (Bob). A secure key could be generated on demand and could be directly used for transactions or stored for future online authentication.

The height for finding horizon of handheld mobile devices (h) = The height of the person holding mobile QKD device(X) + Height of the platform person standing from sea level (H)

The equation (1) derived earlier can be transformed for the scenario as below

$$3.570\sqrt{h}$$

,Where h is the height from sea level

Horizon OG =  $3.570\sqrt{h}$  , Where h = H + X . So that horizon when a person holding hand held Quantum key distribution device is

$$3.570\sqrt{H + X}$$

**IX. THE OPERATIONAL RANGE OF QUANTUM CRYPTOGRAPHIC DEVICES WHEN USING ON THE DIFFERENT TYPE OF NAVAL VESSEL**

*A. Aircraft Carrier*

Largest naval vessel type existing now is aircraft carrier. The height and width of the carrier largely varies according to the class of the carrier but this type of ship can be tall as 200 feet and 120 to 250 feet width[12], wide to enable aircraft to take off and land, and they include space for storing and maintaining planes as well as housing a large crew.

The maximum possible height of any quantum cryptographic devices can be calculated by the feature of largest naval vessel existing now.

Largest naval vessel type: Aircraft carrier [13]

Name: USS Theodore Roosevelt

Length :332.8Meter

Width : 76.8Meter, Which includes flight deck. The USS Theodore Roosevelt (CVN-71)was entered the service on 1986. It is the fourth in US Navy’s Nimitz class of nuclear powered aircraft carriers and has a maximum speed of more than 34 MPH( Miles per Hour) and can remain at sea for up to 25 years.

The height and width of this type of Aircraft carrier largely varies according to the class of the carrier and this type of ship is tall as 61 Meter and upto 80 meter width[12], wide to enable aircraft to take off and land, and they include space for storing and maintaining planes and crews in large numbers and needs for the survival in long.



Figure 6- USS Theodore Roosevelt

The horizon of quantum cryptographic link possible of this largest naval vessel(aircraft carrier) is equal to  $3.570\sqrt{h}$  ,Where h is the height of the aircraft carrier from sea-level and Aircraft carrier usually as tall as 200 feet with the width of 120 to 250 feet .We know that 200ft approximately equals

60.96 Meters, so the answer is

$$3.570\sqrt{60.96} = 27.88 \text{ Kilometer (KM)}$$

$$\text{Area of a Circle} = \pi r^2$$

So the operational circular area of a Quantum Key Distribution devices around aircraft carrier can be calculated as

$$\begin{aligned} &= 3.14 * (27.88)^2 \\ &= 2440.70 \text{ Km}^2 \end{aligned}$$

**B. Small Category Naval Vessels**

Consider that, usually this type of vessels can be categorized as tall as up to 50 feet, we can calculate that 50 Feet approximately equals 615.24 Meters, so the Line of Sight is

$$3.570\sqrt{15.24} = 14 \text{ Kilometer (KM)}$$

So the operational circular area of a Quantum Key Distribution devices around a small naval vessel up to 50 Feet height can be calculated as

$$\begin{aligned} \text{Area of a Circle} &= \pi r^2 \\ &= 3.14 * (14)^2 = 615 \text{ Km}^2 \end{aligned}$$



Figure -7 Small Naval Ship

**C. Experimental Verification of Line of Sight of a vertically polarized Light while using in a small Ocean vessel**

We have experimentally tested Line of sight of a vertically polarized beam using a LASER light and a vertical polarizer using an Ocean vessel with height of 10 Feet approximately equals 3.048 Meters, as

$$3.570\sqrt{3.048} = 6.23 \text{ Kilometer (KM)}$$

$$\text{Area of a Circle} = \pi r^2$$

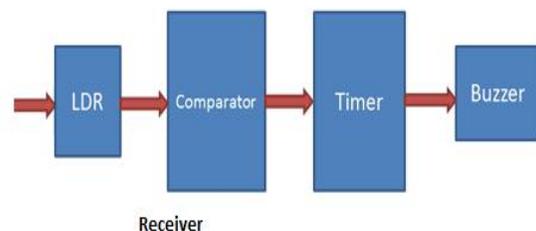
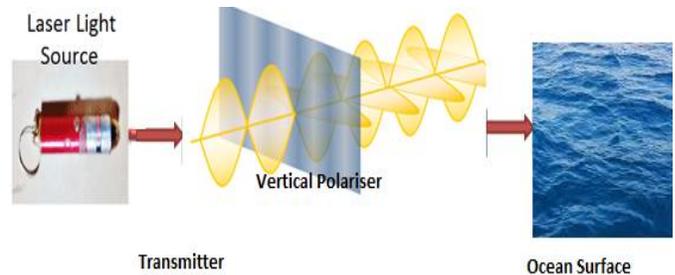
So the operational circular area of a Quantum Key Distribution devices around a small naval vessel up to 20 Feet height can be calculated by equation,

$$\begin{aligned} \text{Area of a Circle} &= \pi r^2 \\ &= 3.14 * (6.23)^2 \\ &= 121 \text{ Km}^2 \end{aligned}$$

The variation of Line of Sight of both measurement on table below can be attributed to the height variation due to tidal waves and Refraction of Light

TABLE 1. Calculation of Line of Sight by Equation and by LASER experiment

Theoretically calculated Line of Sight of a Vertically Polarized Laser Light in a 10 Feet Height Small Naval Vessel using equation	Experimentally Obtained Line of Sight of Vertically Polarized Laser Light in a 10 Feet Height Small Naval Vessel (Average of 5 times Measurement)
$3.570\sqrt{3.048} = 6.23$ Kilometer	6.54 Kilometers



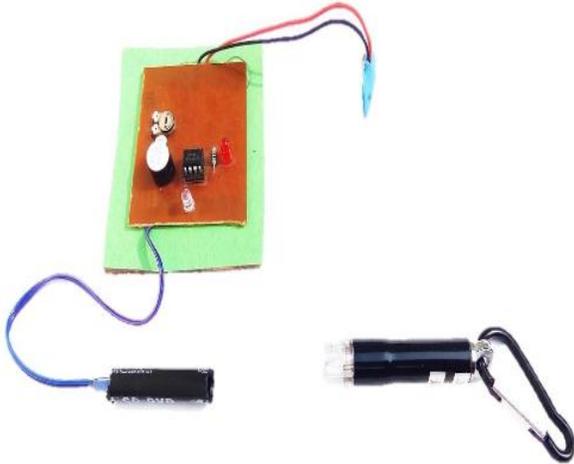


Figure 8 – Simple LDR Based Vertical Polarized Laser Beam Detection System over Ocean surface

**X. TRANSMISSION POWER LOSS CALCULATION OF QUANTUM CRYPTOGRAPHY LINK BETWEEN NAVAL VESSELS**

The intention of this section is for developing the various parameters like signal Attenuation, Data rate that necessary for calculating the performance of the polarized photon based optical communication link[13]. We can consider the situation of optical link between points in free-space above ocean.

Consider a laser device of Quantum cryptography link transmitting a polarized light with total power  $P_T$  at the wavelength (650, 785, 1550) nm. The signal power received at the communications detector can be expressed as below equation,

$$P_R = P_T \frac{D^2}{\theta^2 L^2} 10^{-\gamma L/10} \tau_T \tau_R$$

where  $D$  is the diameter of receiver,  $\theta$  is the divergence angle,  $\gamma$  is the atmospheric attenuation factor in Decibel per Kilometer(dB/km),  $\tau_T$ ,  $\tau_R$  are the transmitter and receiver optical efficiency respectively.

**A. Link Margin and Data Rate**

Another critical parameter in optical communications link analysis is the "Link Margin", which can be termed as ratio of available received power to the receiver power required to achieve a specified Bit Error Rate[BER] at a given data rate. Note that the required power at the receiver  $P_{REQ}$  (watts) to

achieve a given data rate,  $R$  (bits/sec), we can define the link margin  $LM$

$$LM = [P_T \lambda / N_b R h c] \times [D^2 / \theta^2 L^2] 10^{-\gamma L/10} \tau_T \tau_R$$

where  $R$  is a data rate,  $h$  is a plank constant and  $c$  is the light velocity. Given a laser transmitter power  $P_{transmitter}$ , with transmitter divergence of  $\theta$ , receiver diameter  $D$ , transmit and receive optical efficiency  $\tau_{transmitter}$ ,  $\tau_{receiver}$  the achievable data rate  $R$  can be obtained

$$R = \frac{P_T P_R 10^{-\gamma L/10} D^2}{\pi(\theta/2)^2 L^2 E_p N_b}$$

where  $E_p = hc/\lambda$ , is the photon energy at wavelength  $\lambda$  and  $N_b$  is the receiver sensitivity (photon/bits) or (dBm).

**XI. CONCLUSION AND FUTURE WORK**

We have successfully calculated horizon for Quantum cryptography link when using in various type of naval vessels. Also successfully verified the theoretical formula using an experimental setup using a polarized photon transmitter and detector . However the theoretical equation for Power loss and Data rate have to be verified for Quantum cryptography link using polarized photons with suitable experimental setup

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